

## MATHEMATICS 360-255-LW

Quantitative Methods II

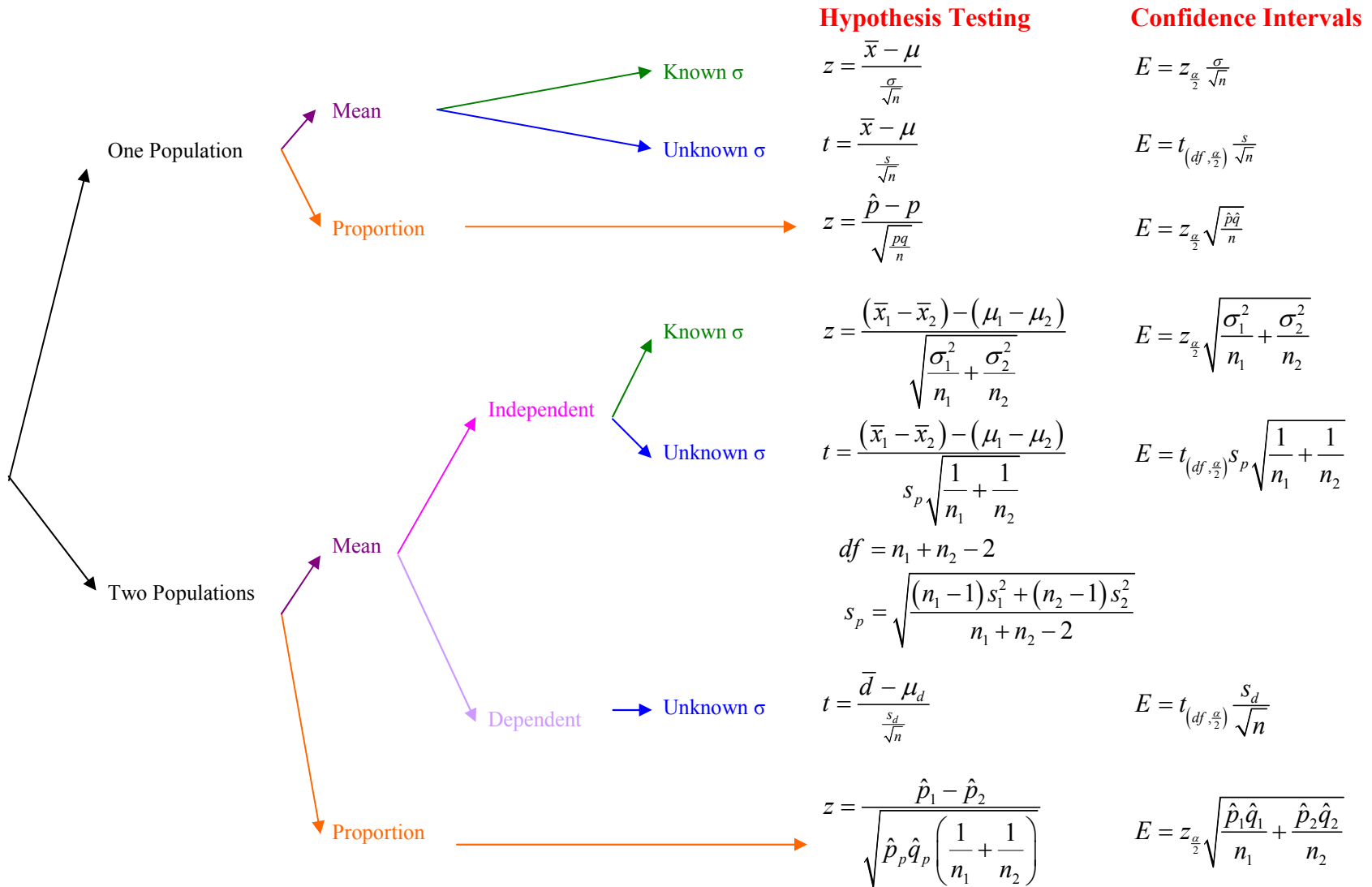
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## Inferences - Steps

	Confidence Intervals	Hypothesis Testing: classical approach	Hypothesis Testing: $p$ -value approach
Step 1	Assumptions	Assumptions	Assumptions
Step 2	a) Identify the probability distribution used (the test statistic). b) Determine the level of confidence, $1 - \alpha$	State the hypothesis $H_0$ : (=) $H_a$ : ( $\neq$ , $<$ or $>$ )	State the hypothesis $H_0$ : (=) $H_a$ : ( $\neq$ , $<$ or $>$ )
Step 3	Find the point estimate	a) Identify the test statistic to be used. b) Determine the kind of test and the level of significance $\alpha$ . (If it is not given, assume $\alpha = 0.05$ ) c) Determine the critical region(s) and the critical value(s).	a) Identify the test statistic to be used. b) Determine the kind of test and the level of significance $\alpha$ . (If it is not given, assume $\alpha = 0.05$ )
Step 4	Determine the confidence interval a) Find the confidence coefficient $z_{\frac{\alpha}{2}}$ or $t_{(df, \frac{\alpha}{2})}$ , or... b) Find the maximum error of estimate $E$ . c) Find the confidence interval: $\bar{x} - E < \mu < \bar{x} + E$	Calculate the value of the test statistic	a) Calculate the value of the test statistic. b) Calculate the $p$ -value
Step 5	Describe the results.	Determine the results a) Is the test statistic in the critical region? b) Make a decision about $H_0$ . From (a): Yes $\Rightarrow$ reject $H_0$ No $\Rightarrow$ fail to reject $H_0$ . c) Write a conclusion.	Determine the results a) Is the $p$ -value less than $\alpha$ ? b) Make a decision about $H_0$ . From (a): Yes $\Rightarrow$ reject $H_0$ No $\Rightarrow$ fail to reject $H_0$ . c) Write a conclusion.

# Inferences – Decision Chart



## Hypothesis Testing

## Confidence Intervals

$$E = z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}$$

$$E = t_{(df, \frac{\alpha}{2})} \frac{s}{\sqrt{n}}$$

$$E = z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}\hat{q}}{n}}$$

$$E = z_{\frac{\alpha}{2}} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$$

$$E = t_{(df, \frac{\alpha}{2})} s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

$$E = t_{(df, \frac{\alpha}{2})} \frac{s_d}{\sqrt{n}}$$

$$E = z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}}$$