

MATHEMATICS 201-510-LW

Business Statistics

Martin Huard

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XVIII – Hypothesis Testing for μ (small samples)

1. The dean of a university claims that the mean time spent partying by all students at this university is less than 7 hours per week. A random sample of 20 students taken from this university showed that they spent an average of 6.2 hours partying the previous week with a standard deviation of 2.3 hours. Assuming the time spent partying by all university students is approximately normally distributed, can you conclude, at the 2.5% significance level, that the president's claim is true? Use the classical approach.
2. A past study claims that adult Canadians spend an average of 18 hours a week on leisure activities. A researcher wanted to test this claim. She took a random sample of 10 adults and asked them about the time they spend per week on leisure activities. Their responses (in hours) are as follows.

14 25 22 38 16 26 19 23 41 33

Assume that the time spent on leisure activities by all adults is normally distributed. Using the 5% significance level, can you conclude that the claim of the earlier study is true? Use the p -value approach.

3. How many pairs of shoes do female college students own? A random sample of 15 female college students produced a sample mean of 8.7 pairs of shoes, with a standard deviation of 0.85 pairs. Use these data to test the claim that the mean number of pairs of shoes owned by female college students is less than 10 at the 5% level of significance. Assume that the number of pair of shoes owned by female students is normally distributed.
 - a) Use the classical approach.
 - b) Use the p -value approach.
4. These are the number of packages handled by a shipping office on 17 randomly selected days.

1103 1488 1713 1536 1037 1462 1625 1627 1547
1080 1216 1639 1539 1545 907 1307 1387

Test the claim that the shipping office handles more than 1200 packages per day at the 1% level of significance. Assume that the number of packages handled by a shipping office in a day is normally distributed.

- a) Use the classical approach.
- b) Use the p -value approach.

5. Major league baseball managers keep a close eye on the “pitch count” of their starting pitcher, because they believe that a pitcher loses his effectiveness after a certain number of pitches. Here are the pitch counts of 16 randomly selected starting pitchers.

117	94	137	66	103	100	81	98
86	77	94	95	115	79	93	86

At the 5% level of significance, test the claim that the mean pitch count for starting pitchers is 100 pitches. Assume that the pitch count for starting pitchers is normally distributed.

- Use the classical approach.
 - Use the p -value approach.
6. A random sample of 20 workers who log on to Yahoo while at work were asked how long they stayed logged on while at work. The mean length was 106 minutes with a standard deviation of 42 minutes. Use this sample to test the claim that the mean time spent on Yahoo is greater than 90 minutes at the 5% level of significance. Assume that the time logged on to Yahoo is normally distributed.
- Use the classical approach.
 - Use the p -value approach.

7. What is wrong with this statistical project?

A student in Business Statistics randomly selects 10 students at SLC, and asks each of them to note the time (in min) it takes them to complete a particular task. Here are the results

10	11	11	12	12	12	13	13	14	68
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She then uses these results to claim that the mean time taken to complete the test is over 10 minutes, using the hypothesis test introduced for this section.

ANSWERS

1. $H_0 : \mu = 7$ hours critical value: $t_{(19,0.975)} = -2.093$ Fail to Reject H_0
 $H_A : \mu < 7$ hours test statistic: $t = -1.556$
2. $H_0 : \mu = 18$ hours test statistic: $t = 2.692$ Reject H_0
 $H_A : \mu \neq 18$ hours $0.022 < p\text{-value} < 0.032$
3. $H_0 : \mu = 10$ pairs of shoes critical value: $t_{(14,0.95)} = -1.761$ Reject H_0
 $H_A : \mu < 10$ pairs of shoes test statistic: $t = -5.923$
 $p\text{-value} < 0.001$
4. $H_0 : \mu = 1200$ packages critical value: $t_{(16,0.01)} = 2.583$ Reject H_0
 $H_A : \mu > 1200$ packages test statistic: $t = 3.329$
 $p\text{-value} = 0.002$
5. $H_0 : \mu = 100$ pitches critical values: $\pm t_{(15,0.025)} = \pm 2.131$ Fail to reject H_0
 $H_A : \mu \neq 100$ pitches test statistic: $t = -1.128$
 $0.248 < p\text{-value} < 0.288$
6. $H_0 : \mu = 90$ min critical value: $t_{(19,0.05)} = 1.729$ Fail to reject H_0
 $H_A : \mu > 90$ min test statistic: $t = 1.704$
 $0.052 < p\text{-value} < 0.053$
7. Because of the number 68, the assumption that the population is normally distributed is probably false. Numbers, such as this 68, that are not consistent with the bulk of the data are called **outliers**. Under certain circumstances, they can be removed and the hypothesis test conducted with the remaining data.