

MATHEMATICS 201-203-RE

Integral Calculus

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Strategy for Testing Series

State the test used to determine the convergence of the following series and make a guess as to whether the series converges or diverges.

a) $\sum_{n=1}^{\infty} \frac{n-1}{n^2+n}$

b) $\sum_{n=1}^{\infty} \frac{3n-2\sqrt[3]{n}}{\sqrt[3]{n^2+5}}$

c) $\sum_{n=1}^{\infty} (-1)^n \frac{2n}{n^2+1}$

d) $\sum_{n=1}^{\infty} \frac{2^n}{n^2+1}$

e) $\sum_{n=1}^{\infty} \frac{\operatorname{arccot}(n)}{n^2+1}$

f) $\sum_{n=1}^{\infty} (\sqrt[n]{2}-1)^n$

g) $\sum_{n=1}^{\infty} \cos n$

h) $\sum_{n=2}^{\infty} \frac{\sin n}{n^5}$

i) $\sum_{n=1}^{\infty} \frac{2(-3)^{2n+3}}{4^{n-1}5^{1-3n}}$

j) $\sum_{n=1}^{\infty} \frac{2^n}{(2n+1)!}$

k) $\sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt{n+1}}$

l) $\sum_{n=1}^{\infty} \frac{4^n}{n+8^n}$

m) $\sum_{n=1}^{\infty} \frac{(-2)^{2n}}{n^n}$

n) $\sum_{n=1}^{\infty} \frac{n^2+1}{n^3-3}$

o)
$$\sum_{n=2}^{\infty} \frac{\sqrt{n^3+1}}{\sqrt[4]{n^3-1}}$$

p)
$$\sum_{n=2}^{\infty} \ln n$$

q)
$$\sum_{n=0}^{\infty} \frac{n!}{2 \cdot 5 \cdot 8 \cdots (3n+2)}$$

r)
$$\sum_{n=1}^{\infty} \frac{e^{\frac{1}{n}}}{n^2}$$

s)
$$\sum_{k=1}^{\infty} \frac{1}{\sqrt{k(k+2)}}$$

t)
$$\sum_{n=1}^{\infty} \frac{(-1)^n n}{2^n (2n)!}$$

u)
$$\sum_{n=1}^{\infty} \frac{\ln n}{n^2}$$

v)
$$\sum_{n=0}^{\infty} \left(\frac{2n}{5+6n} \right)^n$$

w)
$$\sum_{n=1}^{\infty} \frac{n+3}{3^n}$$

x)
$$\sum_{n=1}^{\infty} \frac{n}{e^n}$$

y)
$$\sum_{n=1}^{\infty} (-1)^n \frac{\sqrt{n}}{\sqrt{n+1}}$$